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Algorithmics: Complexities and times

# LAB 1

**VECTOR 1 MEASUREMENTS*:***

The following measurements corresponds to the different methods in *Vector1*.

|  |  |  |  |
| --- | --- | --- | --- |
| n | fillIn (micros) | sum (micros) | maximum (micros) |
| 10 | 0,3100 | 0,0062 | 0,0124 |
| 50 | 1,1000 | 0,0343 | 0,0328 |
| 250 | 4,5200 | 0,2091 | 0,1638 |
| 1250 | 22,4600 | 0,9400 | 0,7349 |
| 6250 | 118,60 | 5,46 | 3,43 |
| 31250 | 680,80 | 26,98 | 18,10 |
| 156250 | 3061,30 | 137,13 | 88,46 |
| 781250 | 14040 | 811,05 | 759,63 |
| 3906250 | 78160 | 3450 | 3916 |
| 19531250 | 408890 | 17223 | 20200 |
| 97656250 | 2205570 | 78000 | 106100 |

As we can see, the fillIn() method takes a lot more time than the other two. The reason for this could be that the fillIn() method creates a new random number for each cell in the array, which takes a lot of resources.

In conclusion, even though the three methods have an O(n) complexity (they iterate through the whole array), their runtime performance differs hugely due to the different operations carried out in each one.

**DIAGONAL 1 MEASUREMENTS*:***

The following measurements corresponds to the different methods in *Diagonal1*.

Now we are dealing with a matrix and the results repeat themselves. The main difference now is that not all the methods have the same complexity. FillIn() and sum1Diagonal() have O(n2) complexities, while sum2Diagonal() has O(n) complexity. This is the reason why sum1Diagonal() is slower than sum2Diagonal(). FillIn() is again much slower than the other two due to the random numbers it generates inside its loops.

|  |  |  |  |
| --- | --- | --- | --- |
| n | fillIn (micros) | sum1Diagonal (micros) | sum2Diagonal (micros) |
| 3 | 0,148 | 0,007947 | 0,002157 |
| 6 | 0,466 | 0,0322 | 0,004559 |
| 12 | 1,759 | 0,0965 | 0,0083 |
| 24 | 6,906 | 0,4011 | 0,0163 |
| 48 | 27,4 | 1,88 | 0,032 |
| 96 | 111,3 | 6,26 | 0,0682 |
| 192 | 442,6 | 21,54 | 0,1464 |
| 384 | 2050 | 77,74 | 0,5491 |
| 768 | 7220 | 288 | 1,14 |
| 1536 | 113660 | 1111 | 1,61 |
| 3072 | 457000 | 4429 | 4,809 |
| 6144 | 1825000 | 17800 | 12,2 |

LAB1 CONCLUSSIONS:

1. *Do the values obtained meet the expectations? For that, you*  
   *should calculate and indicate the theoretical values of the*  
   *complexity for all the methods.*

Vector1 theoretical values, based on the first measurement for n = 10, are calculated via the equation:

T2 = (n2/n1) \* T1

Thus, the results are the following:

|  |  |  |  |
| --- | --- | --- | --- |
| n | fillIn (theor) | sum (theor) | maximum (theor) |
| 10 | 0,31 | 0,01 | 0,01 |
| 50 | 1,55 | 0,03 | 0,06 |
| 250 | 7,75 | 0,16 | 0,31 |
| 1250 | 38,75 | 0,78 | 1,55 |
| 6250 | 193,75 | 3,88 | 7,75 |
| 31250 | 968,75 | 19,38 | 38,75 |
| 156250 | 4843,75 | 96,88 | 193,75 |
| 781250 | 24218,75 | 484,38 | 968,75 |
| 3906250 | 121093,75 | 2421,88 | 4843,75 |
| 19531250 | 605468,75 | 12109,38 | 24218,75 |
| 97656250 | 3027343,75 | 60546,88 | 121093,75 |

Compared with the actual times, we have this graphs:

As we can see, in fillIn() and maximum() the theoretical times were higher than the actual times, while in sum() it was the other way around.

Diagonal1 theoretical values are calculated via the equation:

T2 = (n22/n12) \* T1

Thus, the results are the following:

|  |  |  |  |
| --- | --- | --- | --- |
| n | fillIn (theor) | sum1Diagonal (theor) | sum2Diagonal (theor) |
| 3 | 0,148 | 0,007947 | 0,002157 |
| 6 | 0,592 | 0,031788 | 0,004314 |
| 12 | 2,368 | 0,127152 | 0,008628 |
| 24 | 9,472 | 0,508608 | 0,017256 |
| 48 | 37,888 | 2,034432 | 0,034512 |
| 96 | 151,552 | 8,137728 | 0,069024 |
| 192 | 606,208 | 32,550912 | 0,138048 |
| 384 | 2424,832 | 130,203648 | 0,276096 |
| 768 | 9699,328 | 520,814592 | 0,552192 |
| 1536 | 38797,312 | 2083,258368 | 1,104384 |
| 3072 | 155189,248 | 8333,033472 | 2,208768 |
| 6144 | 620756,992 | 33332,13389 | 4,417536 |

Comparing with the actual times, we have these graphs:

As we can see, here the difference are much bigger and fillIn() and sum2Diagonal() perform worse than they should theoretically, while sum1Diagonal performs better.

1. *What are the main components of the computer in which you*  
   *did the work?*

Most of the work was done by the processor, in charge of doing the operations inside the loops. The memory also worked, but not as hardly.

Out of curiosity, I ran maximum() from Vector1 while I watched over the Windows task manager. In my computer, the CPU usage increased from 1% (in rest) to 30%, and the memory usage only increased from 39% to 42%. Running the methods in Diagonal2, however, only raised my CPU up to 28% and didn’t raise my memory usage at all.

# LAB 2

**TABLE1: TWO ALGORITHMS WITH THE SAME COMPLEXITY**

This table shows the values obtained for the executions of loop2 and loop3, both O(n2) algorithms.

|  |  |  |  |
| --- | --- | --- | --- |
| n | loop2(micros) | loop3(micros) | loop2(micros)/loop3(micros) |
| 1 | 0,0930 | 0,0940 | 0,9894 |
| 2 | 0,1410 | 0,1560 | 0,9038 |
| 4 | 358,0000 | 390,0000 | 0,9179 |
| 8 | 1,1550 | 1,1650 | 0,9914 |
| 16 | 4,4780 | 4,5590 | 0,9822 |
| 32 | 17,6480 | 17,7100 | 0,9965 |
| 64 | 0,0699 | 0,0702 | 0,9957 |
| 128 | 287 | 285 | 1,0060 |
| 256 | 1134 | 1113 | 1,0184 |
| 512 | 4432 | 4545 | 0,9751 |
| 1024 | 21800 | 17853 | 1,2211 |
| 2048 | 107900 | 73400 | 1,4700 |
| 4096 | 324800 | 290200 | 1,1192 |
| 8192 | 1265800 | 1148300 | 1,1023 |
| 16384 | 5026000 | 4572000 | 1,0993 |

The corresponding graphs are:

The results make sense with the complexity of the loops.The graph shows quadratic functions both for loop2 and loop3. By dividing loop2/loop3 times, we get the implementation constant, which tells us which loop performs better given n. Loop3 is better from n = [1024,4096], but then both loops perform more or less equally.

**TABLE2: TWO ALGORITHMS WITH DIFFERENT COMPLEXITY**

Now we compare an O(n logn) algorithm, loop1, with an O(n2) algorithm, loop2.

|  |  |  |  |
| --- | --- | --- | --- |
| n | loop1(micros) | loop2(micros) | loop1(micros)/loop2(micros) |
| 1 | 0,110 | 0,093 | 1,183 |
| 2 | 0,140 | 0,141 | 0,993 |
| 4 | 0,343 | 0,358 | 0,958 |
| 8 | 1,170 | 1,155 | 1,013 |
| 16 | 4,692 | 4,478 | 1,048 |
| 32 | 17,806 | 17,648 | 1,009 |
| 64 | 68,700 | 69,900 | 0,983 |
| 128 | 284,400 | 286,700 | 0,992 |
| 256 | 1185 | 1133,500 | 1,045 |
| 512 | 4604 | 4432 | 1,039 |
| 1024 | 18700 | 21800 | 0,858 |
| 2048 | 76400 | 107900 | 0,708 |
| 4096 | 301200 | 324800 | 0,927 |
| 8192 | 1199900 | 1265800 | 0,948 |
| 16384 | 4652000 | 5026000 | 0,926 |

The graphs are:

Here, the difference between one algorithm and the other does not seem too obvious, but in the table we can see how with big numbers ( n > 16384) the difference would grow bigger and bigger. O(n logn) would show itself faster than O(n2). For n = [1024, 2048] the implementation constant shows that loop1 is much faster.

**TABLE3 == TWO ALGORITHMS WITH DIFFERENT COMPLEXITY:**

I was asked to create loop4, an O(n4) algorithm, and loop5, an O(n3) algorithm and obtain the following table and graphs:

|  |  |  |  |
| --- | --- | --- | --- |
| n | loop4(micros) | loop5(micros) | loop4(micros)/loop5(micros) |
| 1 | 0,1250 | 0,0940 | 1,3298 |
| 2 | 0,3430 | 0,3740 | 0,9171 |
| 4 | 4,5270 | 3,7600 | 1,2040 |
| 8 | 70,2 | 35,9 | 1,9554 |
| 16 | 1250 | 357,2 | 3,4994 |
| 32 | 18410 | 3417 | 5,3878 |
| 64 | 297000 | 31200 | 9,5192 |
| 128 | 4617000 | 294800 | 15,6615 |
| 256 | 74585000 | 2621000 | 28,4567 |

The results are smashing: loop4 rises way higher than loop5 even with small numbers of n (n > 128). This proves how important algorithm complexity is, and just how bad an O(n4) complexity is. The implementation constant is also clear: for every value, loop5 performs better than loop4.

Extra question: *What is the complexity of the method contained in Unknown? Why?*

The complexity of unknowned() is O(n3) because it has three nested loops, each of which is proportional to n.